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# CONTENT BIOLOGICAL SCIENCES

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### **TECHNICAL SCIENCES**

### AN ERROR OF 3-DIMENSIONS DIGITAL INTEGRATOR OF SEQUENTIAL CARRY INTERPOLATOR IN TASKS OF COMPUTER GRAPHICS

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#### **Abstract**

A study and analysis of features of recreation of segments of straight lines are undertaken after the method of digital differential analyzer in a linear interpolator, the errors of DDA and 3-dimentions linear interpolation are certain with the use of digital integrator of sequential carry.

**Keywords:** computer graphics, graphic information, line, 3-dimensions linear interpolation, error, digital differential analyzer, digital integrator of sequential carry, pulse rate multipler

An important task of computer technology is the information service of human life, which is expressed, in particular, in the use of information display devices, which are an integral part of various computer systems, systems and networks. Many multidimensional parameters of real objects require an increase in the number of measurements, increasing the speed of information output and the accuracy of information reproduction by display devices. The most informative and visual way of presenting information is graphical, which is associated with physiological, biological and psychological features of human perception of information as an active part of various computer systems. In addition, there is a tendency to increase the share of information in graphical two-dimensional (2D) and three-dimensional (3D) forms in real time in information measurement systems, research, industry, etc.. All this makes the issue of synthesis of graphic information display devices, which provide the maximum achievable performance with a minimum of hardware costs for their implementation. Large information flows for information display devices require compression, which allows you to optimize the operation of it. Information recovery is based on interpolation algorithms, usually linear. The most widespread elements of the three-dimensional (3D) graphic stages are flat grounds, triangles and segments of straight lines [2, 7, 10, 11]. As a task of recreation of grounds and triangles (both filled by a color and contour [3, 7, 10, 11]) can be broken up on the row of tasks on the recreation of segments of straight lines, then it is possible to consider the segment of straight line the basic element of images.

**Raising of task.** Among the methods of linear interpolation on the recreation of segments of straight lines most distribution was got by the methods based on the use of digital integrators of sequential carry, and methods that is based on the use of digital integrators of parallel transfer or with the calculation of criterion function, Bresenham's line algorithm (BLA) [2, 6, 9, 11].

One bresenham algorithm for a line in 2D space such [9, 11]:

```
{\\\\\\\\brace bresenham algorithm ////////} procedure bresenham (x1, y1, x2, y2, value: integer);
```

```
var dx, dy, iner1, iner2, d, x, y, xend: integer;
     begin
     dx := abs (x2 - x1);
    dy := abs (y2 - y1);
    d := 2*dy - dx; { start value of d }
     incr1 := 2*dy; { constant for increment step, if d
     incr2 := 2*(dy - dx); { constant for increment
step, if d \ge 0
     if x1 > x2
     then { start at minimum x-value point }
    begin
    x := x2;
    y := y2;
     xend := x1
    end
    else
    begin
    x := x1;
    y := y1;
     xend := x2
    end
     write_pixel (x, y, value) ; { first point of line }
     while x < xend do
    begin
     x := x + 1;
     if d < 0
     then
    d := d + incr1 \{ choice of si, y - does not change \}
     begin
    y := y + 1; { choice of ti, y - increases }
     d := d + incr2
    end
     write_pixel (x, y, value) { the line chosen near-by
is a point }
    end { end of while }
```

Linear interpolation devices, systems of differential equalizations of line based on a decision in a self-reactance kind with the use of digital integrators of parallel transfer, two contain register of increases and two story summators. The module of enumeration of summators equals  $2^n$ , where a n-bit of summators is.

{//////// bresenham algorithm \\\\\\\\\}

As single increases on coordinates come forward signals of summator repletion signal. The linear interpolator based on the decision of the system of differential equalizations of line in a self-reactance kind with application of digital integrators of sequential carry is contained by two register of increases (RG<sup>x</sup>, RG<sup>y</sup>), two pulse rate multipler (PRM) and general for both integrators counter – CT (fig.1) [1, 2, 10].

Signals of exits of pulse rate multipliers are the signals of single increases on coordinates. Application of integrators of sequential carry brings in an additional error through the unevenness of passing of impulses on the exit of integrator, that can be decreased, for example, using the combined digital integrators. The abovementioned methods interpolate the arbitrary segment of line for  $2^n$  times, where a n-bit of device is. To increase the fast-acting of linear interpolation, change the capacity of counter of binary multiplier depending on the sizes of coordinate increases or carry out the common increase of co-ordinate increases to normalization of

one of them (carry out the change of both coordinate increases aside most significant digits, that the most significant digit of one of coordinate increases coincided with the most significant digit of device).

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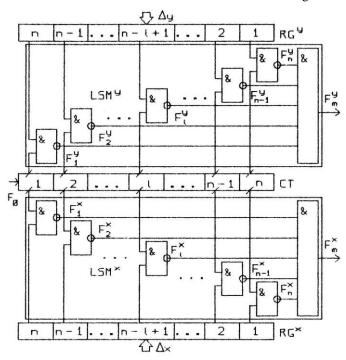


Fig.1. Two-dimensional linear interpolator is on the basis of digital differential analyzer.

The feature of BLA-method is an exception of increase operation of functional dependence of X and Y due to the use of step-by-step algorithms that change increase operation in the function of y=f(x) on the step-by-step operations of addition. Interpolation on it method gives a ordinate error that does not exceed the step of discretisation. Well-known BLA-method, that will realize co-ordinate steps as soon as, so diagonal steps [2, 10]. Also there are BLA-methods, that interpolations (not more than 0.5 step of discretisation) give a minimum ordinate error. A method found application with the calculation of two BLA-method functions and side-step less. Methods that will realize two co-ordinate steps are known also.

Research actuality is conditioned by swift development of computer graphics facilities for the recreation of difficult pictures and stages with the large dynamics of image [2,10], in that the various high-performance algorithms of recreation of images elements are widely used with the aim of increase of the productivity and reduction of hardware expenses [2,10].

Exactly defined errors of digital differential analyzer (DDA) and 2D-linear interpolation by digital integrator of sequential carry (DISC) [2, 10].

An aim of the article is an analysis of features of algorithm of recreation of segments of straight lines after the method of DDA for determination of error of linear interpolation at the recreation of information in three-dimensional discrete co-ordinate space.

### Analysis of features of digital differential analyzer work.

Digital integrator of sequential carry is known, as pulse rate multipler (PRM) [12] and also, as a digital differential analyzer. The name "pulse rate multipler"

arose up in connection with the use of him as a transcoder in frequency. If on the entrance of counter of PRM to give pulse of permanent frequency string, then on the exit of PRM there will be present impulses with a midfrequency, what proportional to the control code.

At the count of impulses amount on going PRM beyond a time that answers beginning and end of period of impulsive sequence domain, there is possible appearance of error on the entrance of counter. An error is related to the unevenness of impulses on a PRM-exit and discrete presentation of count result. Unevenness of passing of impulses on a PRM-exit expressed in that between the following of impulses one is after one on a PRM-exit different intervals at an unchanging control code and even entrance frequency on the entrance of counter. In digital integrators in general and in DISC in particular replacement of integration operation of xfunction (x = f(t)) on the summarization operation of successive values of  $x_k(t_k)$ -functions. Successive values are set in the discrete points of  $t_k$ , thus  $t_{k+1}$ - $t_k$ = $\Delta t$ ;  $\Delta t$  is permanent, does not depend on  $t_k$  and proportional single impulses, id est cost of impulses that act on the entrance of integrator equals "1" [1]. The error of DISC equals a difference between the value of initial size of x at ideal implementation of the set operation of recreation and size of  $x_0$ , got from signals that seem integrator [1].

Digital integrator gives out a value for the calculation of ordinates of functions in discrete points, that is why an error is examined exactly in these points at the integer values of argument that is measured by the number of impulses [1].

The initial state of DISC-counter (CT) equals "0". In the control code register of DISC (RG) the entered number:

$$\Delta x = \sum_{i=1}^{n} 2^{n-i+1} a_{n-i+1} , \quad (1)$$

where  $a_i$  - i-digit of control code register RG.

The number of impulses, mine-out by the i-chart of coincidence on the receipt of t impulses on the entrance of DISC, equals:

$$t_i = ent\left(\frac{t+2^{i-1}}{2^i}\right),\tag{2}$$

The number of impulses on the DISC-exit equals:

$$x_0 = \sum_{i=1}^{n} t_i a_{n-i+1} .$$
(3)

After the receipt of  $t=2^n$  impulses of DISC pass to the initial state. Equalization of line that passes through points  $(\theta, \theta)$  and  $(2^n, \Delta x)$ :

$$x = \sum_{i=1}^{n} 2^{n-i+1} a_{n-i+1} \cdot t / 2^{n} . \tag{4}$$

Thus, the error of integration of DISC equals  $\mathcal{S}_p = x - x_0$  and looks like :

$$\delta_p = \frac{\sum_{i=1}^n 2^{n-i+1} a_{n-i+1}}{2^n} \cdot t - \sum_{i=1}^n t_i a_{n-i+1} . (5)$$

Consider the three-dimensional (3D) interpolation of the linear function z = f(x, y) on a device that contains three DISC with one common counter (fig.2, 3) [2, 10].

Fig. 4 shows the operation of a 3D linear interpolator on the digital integrator of sequential carry for  $\Delta x = 14$ ,  $\Delta y = 7$ ,  $\Delta z = 11$  (n = 4), which explains the process of constructing the interpolation curve  $z_o = f(x_o, y_o)$  in 3D discrete coordinate display space.

For the horizontal we take x, for the vertical - y, for the third coordinate, which is directed from the observer into the screen of the information display device (IDD), - z. The coordinate axes *Ox*, *Oy*, *Oz* form the left triple [4, 5, 8, 10].

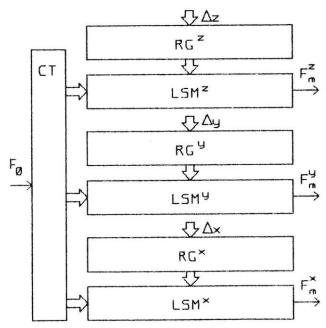


Fig.2. Block diagram of 3D linear interpolator on digital integrator of sequential carry

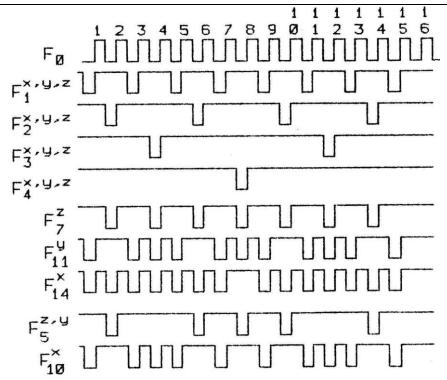


Fig.3. Diagrams signals examply of 3D linear interpolator on digital integrator of sequential carry (n = 4)

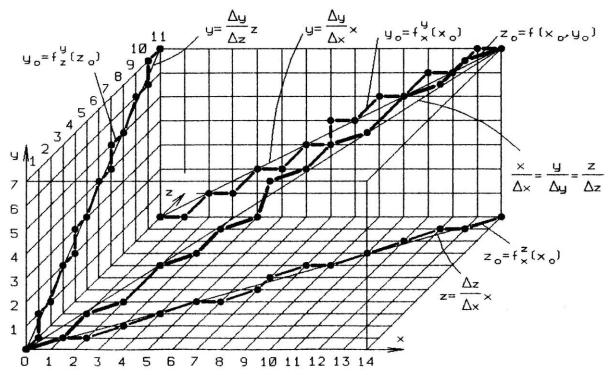


Fig. 4. Operation of a 3D linear interpolator on the digital integrator of sequential carry for  $\Delta x = 14$ ,  $\Delta y = 7$ ,  $\Delta z = 11$  (n = 4)

The codes of the corresponding coordinate increments are written in the control registers of the interpolator:  $\Delta x$  - coordinate increment on the x-axis - in  $RG^x$ ,  $\Delta y$  - on the y-axis - in  $RG^y$ ,  $\Delta z$  - on the z-axis - in  $RG^z$ :

$$\begin{cases} \Delta x = \sum_{i=1}^{n} 2^{n-i+1} a_{n-i+1} \\ \Delta y = \sum_{i=1}^{n} 2^{n-i+1} b_{n-i+1} \end{cases}$$

$$\Delta z = \sum_{i=1}^{n} 2^{n-i+1} c_{n-i+1}$$
(6)

where  $a_i$ ,  $b_i$  or  $c_i$  - i-th digit of  $RG^x$ ,  $RG^y$  or  $RG^z$ , respectively.

The output frequency sequences of the coordinate binary multiplier  $F_m^x$ ,  $F_m^y$  and  $F_m^z$  are respectively functions  $x_0$ ,  $y_0$  and  $z_0$  from the pulses t of the frequency  $F_o$  at the input of the common counter (7):

$$x_0 = \sum_{i=1}^{n} t_i a_{n-i+1}; y_0 = \sum_{i=1}^{n} t_i b_{n-i+1}; z_0 = \sum_{i=1}^{n} t_i c_{n-i+1}.$$
 (7)

As a result, we obtain the function  $z_0 = f(x_0, y_0)$  in 3D discrete coordinate space (DCS) (xyz). In the following considerations, we assume that  $\Delta x > = \Delta y$ ,  $\Delta x > = \Delta z$  and  $\Delta x$  contains in the higher digit "1", ie is a normalized value, as the following function is required:

$$\frac{x}{dx} = \frac{y}{dy} = \frac{z}{dz} \quad (8)$$

For the error of 3D linear interpolation at the point  $Q_o(x_o, y_o, z_o) = Q(r_0)$  it is accepted to choose the distance from the point  $Q_o$ ,, which belongs to the 3D discrete coordinate space, on the interpolation curve  $z_o = f(x_o, y_o)$ , to the line is interpolated and given by expression (8)

[2, 4]. That is, for the 3D linear interpolation error  $\delta_o$ , the value of the normal from the point  $Q_0$  to the interpolated line is chosen. Define the expression for  $\delta_n$ .

Assume that the point  $Q_1$   $(x_1,y_1,z_1)$  is the starting point of the segment of the interpolated line, given by the coordinate increments  $\Delta x$ ,  $\Delta y$ ,  $\Delta z$ , and  $Q_2(x_2,y_2,z_2)$  is the end point. The equation of the line passing through the two points  $Q_1$  and  $Q_2$  (9):

$$\frac{x - x_1}{x_2 - x_1} = \frac{y - y_1}{y_2 - y_1} = \frac{z - z_1}{z_2 - z_1}$$
(9)

The distance  $\delta_n$  from the point  $Q_o(x_o, y_o, z_o)$  to the line given by expression (9) is as follows [2, 4]:

$$\delta_{n} = \frac{\sqrt{\begin{vmatrix} y_{2} - y_{1} & z_{2} - z_{1} \end{vmatrix}^{2} + \begin{vmatrix} z_{2} - z_{1} & x_{2} - x_{1} \end{vmatrix}^{2} + \begin{vmatrix} x_{2} - x_{1} & y_{2} - y_{1} \end{vmatrix}^{2}}{\sqrt{(x_{2} - x_{1})^{2} + (y_{2} - y_{1})^{2} + (z_{2} - z_{1})^{2}}}$$
(10)

To simplify the calculations, assume that the point  $Q_1(x_1,y_1,z_1)$  coincides with the origin  $O(x_1=0)$   $y_1=0$ ,

 $z_1$ =0). Then, taking into account (8) and (9), expression (10) takes the form:

$$\delta_{n} = \frac{\sqrt{\begin{vmatrix} \Delta y & \Delta z \end{vmatrix}^{2} + \begin{vmatrix} \Delta z & \Delta x \end{vmatrix}^{2} + \begin{vmatrix} \Delta x & \Delta y \end{vmatrix}^{2}}}{\sqrt{\Delta x^{2} + \Delta y^{2} + \Delta z^{2}}}$$
(11)

It should be noted that the value of  $\delta_n$  can be determined from other dependences [1, 5], but they contain ars-trigonometric functions, which makes it difficult to use such dependences in machine analysis. In turn, the use of (11) allows us to determine only the absolute value of  $\delta_n$ , which fully satisfies the problem of estimating  $\delta_n$ .

The algorithm for determining  $\delta_n$  for  $i=1\div 5$ . program lddn;

{ ------ turbo pascal /15.06.2021/

 $\{determination \ of \ my\text{-mi maximum normal errors}\}$ 

{ 3d linear interpolator on binary multipliers, for } { non-zero values of control code bits, }

 $\{$  and the corresponding values of increases on the y and z axes  $\}$ 

{ at normalized x (in senior discharge "1")}

{ sound signal issuance at the end of the table and page }

{ definition}

{absolute time for calculating the page and table } uses printer,dos,crt;

label aa,bb;

const

rng = 8; { interpolator bit }

bnn = 256; { 2 \*\* rng }

spn = 2; {number of spaces between lines}

mx = 12; {maximum number of records in a row}

my = 1; {number of maximum errors for dx, dy

data]

nl = 30; {number of records per page}

type

vecte =array [1..mx,1..my] of real;

vectz =array [1..mx,1..my] of longint;

```
vectorm=array [1..rng,1..bnn] of integer;
                                                               begin
     vectorb=array [1..rng] of integer; {delete binary
                                                               index:=1;
                                                               nnf:=1;
code }
     vectors = array [1..bnn] of integer; {coordinate
                                                               while index<=nf do
                                                               begin
steps }
                                                               nnf:=nnf*2;
                                                               index:=index+1;
     lps:integer;
                                                      {
*************
     lpg: integer; {number of lines in result page}
                                                               bindegre:=nnf;
     pfn: integer; {number of the first page of the re-
                                                               end
sult }
                                                               else
     pgn: integer; {page number}
                                                               bindegre:=1;
     vstx: longint; {initial value of record argument
                                                               end:
                                                                {/////// degree function with basis 2 \\\\\\\}
(delta x)
     vspx: longint; {final value of writing argument
                                                                {\\\\\\\\ output of the general table cap ////////}
(delta x)}
                                                               procedure prntbtit(var bfl:text); {result file}
     vsty: longint; {initial value of record argument (y
                                                               begin
delta)}
     vspy: longint; {final size of record argument (y
                                                               writeln(bfl,
                                                               'result of ldd7'.
delta)}
     xbin: vectorb; {dx binary code}
                                                               '(turbo pascal version /12.01.2021/)');
     ybin: vectorb; {dy body code}
                                                               writeln(bfl, '3d bin rate multiplier',
     zbin: vectorb; {dz binary code}
                                                               'line interpolator',
     ntd: integer; {number of records per line}
                                                               my,
     h, m, s, f: word; {hours, minutes, sec., hundreds
                                                               ' max errors array');
sec. current time}
                                                               writeln(bfl,' range of interpolator: ',
     ph, pm, ps, pf: word; {hours, min., sec., hundred
                                                               rng: round(ln(rng)/ln(10)+0.5));
sec. beginning of page }
                                                               writeln(bfl);
     th, tm, ts, tf: word; {hours, min., sec., hundred sec.
                                                                {/////// output of the general table cap \\\\\\\}
home off table }
     dh, dm, ds, df: word; {delta hours, minutes, sec-
onds and hundreds of seconds}
                                                               {\\\\ translation into the binary code of the decimal
     vdtx: longint; {number of recording argument val-
                                                          number ////}
                                                               procedure decbintr (date: longint; {decimal num-
ues adjustable)}
     vdty: longint; {number of recording argument val-
                                                          ber}
                                                               var bufarray: vectorb); {b-cod border sequence}
ues (adjustable)}
     pgd: integer; {number of result pages}
     lin: text; {result file}
                                                               index: integer; {binary code bit index}
     lct: integer; {line counter in page}
                                                               bufdate: longint; {translation buffer}
     emax: vecte; {ntd for 8 maximum errors}
                                                               begin
     zmax: vectz; {dz maximum errors}
                                                               index:=1;
     dt: longint; {number of recording argument values
                                                               bufdate:=date;
(initial)}
                                                               while index<=rng do
     nct: integer; {column counter in records}
                                                               begin
     dy: longint; {y increase corresponding to max.
                                                               bufarray[index]:=round
                                                               ((bufdate/2-trunc(bufdate/2))*2);
     dz: longint; {increase in z, corresponding to max.
                                                               bufdate:=trunc(bufdate/2);
                                                               index:=index+1;
     dnm: real; {maximum normal error of delta data}
                                                               end;
     srng: vectorm; {matrix of discharge weight steps}
                                                               end;
     sx: vectors; {x-step step sign, 0-no step, 1-step}
                                                                {/////// translation into the binary code of the dec-
     sy: vectors; {sign of step on the y axis, 0-no step,
                                                          imal number \\\\\\\}
1-step}
     sz: vectors; {z-axe step sign, 0-no step, 1-step}
                                                                {\\\\\\\ zeroing of all bits of the binary code
     x: integer; {record column number}
                                                          ////////}
                                                               procedure binreset (var bufarray: vectorb); {bi-
     {\\\\\\\ degree function with basis 2 ////////}
                                                          nary code sequence}
     function bindegre(nf:integer):longint;
                                                               index:integer;
     nnf:longint;
                                                               begin
     index:integer;
                                                               index:=1;
     begin
                                                               while index<=rng do
     if nf>0 then
                                                               begin
```

```
bufarray[index]:=0;
                                                               end:
     index:=index+1;
                                                               indexi:=1;
                                                               for indexi:=1 to rng do
     end;
    end;
                                                               begin
                                                               bufkk:=round(bnn/bindegre(indexi)-1);
     {/////// zero all bits of binary code \\\\\\\\}
                                                               for indexk:=0 to bufkk do
     {\\\\\\\ "obtaining a coordinate interpolation se-
                                                               begin
quence ////////}
                                                               bufm[indexi,(bindegre(indexi-1) + bindegre(in-
     procedure stepdelt(srng:vectorm;
                                                          dexi)*indexk)]:=1;
     bufb:vectorb:
                                                               end:
     var bufs:vectors);
                                                               end:
    label label1:
                                                               end:
     var
                                                               {/////// getting discharge weight sequences
     indexes: integer; {draft weight matrix row index}
                                                          \\\\\\\}
     index: integer; {binary code column index}
     indexl: integer; {step column index or}
                                                                {\\\\\\\ increasing binary code by one ////////}
     {discharge weight matrix column index}
                                                               procedure bininc (var bufarray: vectorb) {b-code
     begin
                                                          binder sequence}
     begin
                                                               label bbii; {procedure label}
     index1:=1;
     while index1<=bnn do
                                                               index: integer; {digital bit code index dy}
     begin
                                                               begin
                                                               index:=1;
     bufs[index1]:=0;
     inc(indexl);
                                                               while index <= rng do {cycle}
                                                               begin {zoom}
    end;
                                                               if bufarray [index] = 0 then \{*****\}
     end;
     indexi:=rng;
                                                               begin {binary}
     indexk:=1;
                                                               bufarray [index]: = 1; {foot}
     label1: if indexk <=rng then
                                                               goto bbii; {code}
                                                               end {bufarray}
     begin
     if bufb[indexk]=1 then
                                                               else {numbers}
                                                               begin {dy}
     begin
                                                               bufarray [index]: = 0; {on}
     for indexl:=1 to bnn do
                                                               index := index + 1; \{unit\}
     begin
                                                               end; {*****}
     bufs[index1]:=bufs[index1]+srng[indexi,index1];
                                                               end; {"+1"}
     end;
     end;
                                                               bbii: end;
     dec(indexi);
                                                                {/////// increasing binary code by unit \\\\\\\}
     inc(indexk);
                                                                {\\\\\\\ output page number ///////}
     goto label1
     end;
                                                               procedure prnpgnum (ppgn: integer; {page num-
                                                          ber}
     end:
     {/////// obtaining a coordinate interpolation se-
                                                               var bfl: text); {result file}
quence \\\\\\\}
                                                               const plps=110;
                                                               var
     {\\\\\\ production of discharge weight sequences
                                                               ndex: integer; {auxiliary}
////////}
                                                               begin
     procedure horsetet (var bufm: vectorm);
                                                               ppgn: = pgn;
                                                               index: = round (plps / 2-4-round (ln (plps) / ln
     indexes: integer; {matrix line index}
                                                          (10)) + 0.5;
     index: integer; {matrix column index}
                                                               while index> = 1 do
     bufkk: integer; {intermediate value, kk = (2 ** n / 
                                                               begin
2 ** i - 1)
                                                               write (bfl, "); {spaces}
     index: integer; {intermediate index}
                                                               index: = index-1; \{******\}
     begin
                                                               end;
                                                               writeln(bfl, ' - ',
     indexi:=1;
     indexj:=1;
                                                               ppgn:round(ln(abs(ppgn))/ln(10)+0.5),
     for indexi:=1 to rng do
                                                                ' -');
     begin
                                                               end;
     for indexj:=1 to bnn do
                                                                {/////// page number output \\\\\\\}
     begin
     bufm[indexi,indexi]:=0;
                                                                {\\\\\\\ output of the header of records and spaces
     end;
                                                          between them ///////}
```

```
procedure printtit (pntd: integer; {number of rec-
                                                              pemax[indexx,indexy]:=0;
ords in a row}
                                                              pymax[indexx,indexy]:=0;
    pvst: longint; {dx first recording in a row}
                                                              indexy:=indexy+1;
    var bfl: text); {result file}
                                                              end;
    const nottitle = 'dz err'; {record hat}
                                                              indexx:=indexx+1;
                                                              end;
    notcount: integer; {line record counter}
                                                              end;
    spacecnt: integer; {spacer counter between rec-
                                                              {/////// zero eight maximum errors and their dy
                                                         \\\\\\\\}
    bufferdx: longint; {dx values for caps}
    begin
                                                              {\\\\\\ sorting 8 max. errors and overwrite them
    notcount:=pntd;
                                                         dy ///////}
    bufferdx:=pvst;
                                                              procedure sortvect (px: integer; {column number}
    while notcount>=1 do
                                                              pdy: longint; { yield increase }
                                                              perm: real; {maximum error for dy}
    begin
     write (bfl, 'dy =', bufferdx: 3); {dx output in record
                                                              var pemax: vecte; {ntd for 8 maximum errors}
                                                              var pymax: vectz); {corresponding to dz}
cap}
    bufferdx := bufferdx + 1;
                                                              label sr1;
    begin
                                                              index1: integer; {index of eight maximum errors}
    spacecnt: = spn;
     while spacecnt> = 1 do
                                                              index2: integer; {intermediate index 8-max. er-
    begin
                                                         rors }
    write (bfl, "); {output spaces between records}
                                                              begin
spacecnt:=spacecnt-1;
                                                              index1:=1;
                                                              while index1<=my do
    end;
    end;
                                                              begin
    notcount:=notcount-1;
                                                              if abs(perm)>=abs(pemax[px,index1]) then
    end;
                                                              begin
    writeln(bfl);}
                                                              index2:=my;
    notcount:=pntd:
                                                              while index2>=index1 do
    while notcount>=1 do
                                                              begin
                                                              pemax[px,index2]:=pemax[px,index2-1];
    begin
    write (bfl, nottitle); {output of the record cap}
                                                              pymax[px,index2]:=pymax[px,index2-1];
                                                              index2:=index2-1;
    begin
    spacecnt: = spn;
                                                              end;
     while spacecnt> = 1 do
                                                              pemax[px,index1]:=perm;
                                                              pymax[px,index1]:=pdy;
     write (bfl, "); {output spaces between records}
                                                              goto sr1;
    spacecnt:= spacecnt-1;
                                                              end;
    end;
                                                              index1:=index1+1;
    end;
                                                              end;
    notcount:=notcount-1;
                                                              sr1: end:
    end;
                                                              {/////// sorting 8 max. errors and overwrite them
    writeln(bfl);
                                                         dy \\\\\\\}
    end;
     {/////// output of the cap of records and spaces
                                                              {\\\\\\\ print pages with eight maximum errors
between them \\\\\\\
                                                         ////////}
                                                              procedure prnsorty (pemax: vecte; {8 maximum
     {\\\\\\\ resetting eight maximum errors and their
                                                         errors }
                                                              pymax: vectz; {corresponding to dz}
    procedure resvect (var pemax: vecte; {ntd for 8
                                                              pntd: integer; {number of records per line}
maximum errors}
                                                              var bfl: text); {result file}
    var pymax:vectz); { dz }
                                                              var
    var
                                                              ix:integer;
    indexx:integer;
                                                              iy:integer;
    indexy:integer;
                                                              begin
                                                              iy:=1;
    begin
                                                              while iy<=my do
    indexx:=1;
    while indexx<=mx do
                                                              begin
                                                              ix:=1;
    begin
                                                              while ix<=pntd do
    indexy:=1;
     while indexy<=my do
                                                              begin
    begin
                                                              write(bfl,pymax[ix,iy]:3,' ');
```

```
write(bfl,pemax[ix,iy]:1:2,' ');
                                                              function lzero (w: word): string; {machine trans-
     ix := ix + 1;
                                                         lation function}
                                                              {representations of size b}
     end;
     writeln(bfl);
                                                              var {symbol with dynamic long}
                                                              s: string; { function variable}
     iy:=iy+1;
                                                              begin {-----}
     end;
                                                              str (w: 0, s); {proc. translation into symbol key}
     end; {/////// print page with eight maximum er-
                                                              if length (s) = 1 then {if length of symbol repre-
rors \\\\\\\\}
     function factplus(arg:longint):longint;
                                                              s := '0' + s; {then increase it by s, i.e. on 1}
     buf:longint;
                                                              lzero: = s; {assign value of function}
     index1:longint;
                                                              end; {----- end of function body -----}
     index2:longint;
                                                              begin {**** home body procedures prntime
     begin
     if arg=0 then factplus:=1 else
     begin
                                                              writeln (bfl, lzero (hour), ':', {hours}
                                                              lzero (minute), ':', {minutes}
     buf:=0;
                                                              lzero (second), '.', {seconds}
     index1:=1;
     while index1<=arg do
                                                              lzero (sec100)); {hundred seconds}
                                                              end; {**** end of body procedure prntime ****}
     begin
     index2:=1;
                                                              {/////// output time to file \\\\\\\\}
     while index2<=index1 do
     begin
                                                              {\\\\\\\ determination of absolute performance
                                                         ///////}
     inc(index2);
     end;
                                                              procedure dtimer (var h1, m1, s1, f1, {hours, min,
     buf:=buf+index2;
                                                         sec., sec. / 100 start}
     inc(index1);
                                                              h2, m2, s2, f2, {hours, min, sec, sec / 100 end}
     end;
                                                              dhp, dmp, dsp, dfp: word); {absolute perfor-
     factplus:=buf;
                                                         mance }
     end:
                                                              var
                                                              dhb, dmb, dsb, dfb: integer; {buffer integer varia-
     end:
                                                         bles}
     {\\\\\\\ display of time ///////}
                                                              {to define the delta sign}
     timwrit procedure (var hour, minute, second,
                                                              begin {****** home body of dtimer proce-
                                                         dure ********
sec100: word);
     function lzero (w: word): string; {machine trans-
                                                              dfb: = f2-f1; {hundredth of a second delta sign de-
lation function}
                                                         tection}
     {representations of size b}
                                                              if dfb <0 then {if f1> f2, then}
     var {symbol with dynamic long}
                                                              begin {their difference is determined}
     s:string; { переменная функции }
                                                              df: = 100-f1 + f2; {transfer of 100 second dis-
     begin {-----}
                                                         charges,}
     str (w: 0, s); {process of translation into symbol
                                                              dsb: = s2-s1-1; {unit loans from second discharge}
key}
                                                              end {when determining the second delta sign}
     if length (s) = 1 then {if symbol length 1,}
                                                              else \{if f1 \le f2, then\}
     s := 0' + s; {then increase it by s, i.e. on 1}
                                                              begin {their difference is determined}
     lzero: = s; {assign value of function}
                                                              df: = f2-f1; \{no loan, \}
     end; {----- end of function body -----}
                                                              dsb: = s2-s1; \{ second delta sign \}
     begin {**** home body timwrit procedure ****}
     write (lzero (hour), ':', {hours}
                                                              if dsb < 0 then {if s1 > s2, then}
     lzero (minute), ':', { minutes }
                                                              begin {their difference is determined}
     lzero (second), '.', {seconds}
                                                              ds: = 60-s1 + s2; {transfer of 60 from discharge
     lzero (sec100)); {hundred seconds}
     end; {**** end of timwrit body procedure ****}
                                                              dmb: = m2-m1-1; {unit loan from minute}
     {////// display of time \\\\\\\}
                                                              end {when determining the mint sign}
                                                              else \{if s1 \le s2, then\}
     begin {if there was a borrow}
     procedure prntime(var hour,
                                                              if dfb <0 then
                                                              ds: = s2-s1-1 {delta seconds including loan}
     minute,
     second,
                                                              else {if there was no loan, then}
     sec100:word;
                                                              ds: = s2-s1; {delta second is not corrected}
     var bfl:text);
                                                              dmb: = m2-m1; \{ delta minute sign \}
                                                              if dmb < 0 then {if m1 > m2, then}
```

```
begin {their difference is determined}
                                                                ty:=0;
     dm: = 60-m1 + m2; {transfer of 60 from hours}
                                                                tz=0:
                                                                index:=1;
     dhb: = h2-h1-1; {unit loans from hours}
     end {when determining the delta sign.}
                                                                while index<=bnn do
     else {if m1 \le m2, then}
                                                                begin
     begin {if there was a borrow}
                                                                tx:=tx+sxb[index];
     if dsb <0 then {minute must be obtained}
                                                                ty:=ty+syb[index];
     dm: = m2-m1-1 {delta minutes including loan}
                                                                tz:=tz+szb[index];
     else {if there was no loan, then}
                                                                bq:=sqr(tx)+sqr(ty)+sqr(tz);
     dm: = m2-m1: {delta minute is not corrected}
                                                                cq:=sqr(dxb-tx)+sqr(dyb-ty)+sqr(dzb-tz);
     dhb: = h2-h1; \{ delta clock sign \}
                                                                dnb:=sqrt(abs(bq-(sqr(aq+bq-cq))/(4*aq)));
     end:
                                                                if dnb>=dnmax then dnmax:=dnb;
     if dhb <0 then {if h1> h2, their difference is deter-
                                                                inc(index);
                                                                end;
mined }
     dh: = 12-h1 + h2 {including the transfer of 12 from
                                                                dnmbuf:=dnmax;
discharges of the day}
                                                                end:
     else \{if h1 \le h2, then\}
                                                                {/////// max. ordinate error linear interpolator
     if dmb <0 then {if there was a loan from the days,
                                                           \\\\\\\\}
it is necessary)
     dh: = h2-h1-1 {get the delta of the hours according
                                                                begin {\\\\\\ beginning of the main program
to the loan}
                                                           ///////}
     else {if there was no loan, then the delta clock}
                                                                writeln;
     dh: = h2-h1; \{no adjustment\}
                                                                writeln ('----- turbo pascal /15.06.2021/ ------
     end; { ******* end of the body of the dtimer
                                                           ');
procedure *******
                                                                writeln ('3d binary rate multipliers line interpola-
     {/////// determination of absolute performance
                                                           tor',
\\\\\\\}
                                                                'normal maximum errors array');
                                                                writeln;
     {\\\\\\\ determination of the number of decimal
                                                                writeln ('introduce number of first page'); {enter
positions of the number ///////}
                                                           from console number}
     function decposit (anydate: longint): integer;
                                                                write ('->'); {first page, if 1 ",}
                                                                readln (pfn); {then the tablet hat is printed,}
                                                                writeln; {otherwise-ordinary page. }
     buffer:longint;
                                                                writeln ('introduce start increment in x axis');
     begin
     if (0<=anydate)and(anydate<=9) then
                                                           {console input}
     buffer:=1
                                                                writeln ('(', (bindegre (rng-1)): decposit (bindegre
                                                           (rng-1)),
     else
                                                                '<= start delta x <=', {*****}
     buffer:=round(ln(abs(anydate))/ln(10)+0.5);
     decposit:=buffer;
                                                                (bnn-1): rng, ')'); {left border}
     end;
                                                                write ('->'); {*****}
     {/////// determination of the number of decimate
                                                                readln(vstx); { delta x }
positions of the number \\\\\\\
                                                                writeln:
                                                                writeln ('introduce stop increment in x axis');
     {\\\\\\ max. ordinate error linear interpolator
                                                           {console input}
                                                                writeln (',', vstx: decposit (vstx), '<= stop delta x
///////}
                                                           <=', {*****}
     procedure normerr (dxb, dyb, dzb: longint;
     sxb, syb, szb: vectors;
                                                                (bnn-1): rng, ')'); {right}
     var dnmbuf: real);
                                                                write ('->'); {boundaries}
                                                                readln(vspx); { delta x }
     tx: longint; {current increase coordinates on ox
                                                                writeln;
axis}
                                                                decbintr(vstx,xbin);
     ty: longint; {current increase coordinates on oy
                                                                vdtx:=vspx-vstx+1;
                                                                pgd:=round(factplus(vdtx)/(mx*nl)+0.49);
axis}
                                                                writeln('!!!!! - attention - !!!!! ');
     tz: longint; {current increase coordinates on oz
                                                                writeln('there are ',pgd:decposit(round(pgd)),
axis}
                                                                ' page of result table ');
     aq, bq, cq: real;
     dnb, dnmax: real; {normal interpolator error}
                                                                writeln;
     index:integer;
                                                                write(' number of page is ',
                                                                (pgd+pfn-1):(decposit(round(pgd+pfn))));
     begin
                                                                gettime (th, tm, ts, tf); {reversed. to the withdrawal
                                                           procedure. times}
     dnm:=0;
     aq := sqr(dxb) + sqr(dyb) + sqr(dzb);
                                                                write (', it is now'); {print text}
     tx = 0;
```

timwrit (th, tm, ts, tf); {display of table start time	prnsortv(emax,zmax,ntd,lin);
on screen}	writeln(lin);
ph: = th; {remembering the beginning hour of	lct:=lct-1;
page calculations}	goto bb;
pm: = tm; {- "- minute -" -}	end;
ps: = ts; {- "- second -" -}	if vsty <vspy td="" then<=""></vspy>
$pf: = tf; \{- \text{"- tens of seconds -" -}\}$	begin
pgn:=pfn;	write (lin, 'end of', pgn: decposit (round (pgn)),
writeln(', start of ',pgn:decposit(round(pgn)), '	'page,'); {end label output}
page ');	write (lin, 'page computating time:'); {pgn pages}
assign(lin,' lin.tab ');	gettime (h, m, s, f);
rewrite(lin);	dtimer (ph, pm, ps, pf, h, m, s, f, dh, dm, ds, df);
if pgn=1 then	ph: = h; {remembering the beginning hour of page
prntbtit(lin) else	calculations}
	pm: = m; {- "- minute -" -}
prnpgnum(pgn,lin);	ps: = s; {- "- second -" -}
horsetet(srng);	$pf: = f; \{-"- tens of seconds -" -\}$
decbintr (vstx, xbin); {translate dx to xbin binary	prntime (dh, dm, ds, df, lin); {output of page time
code [irng]}	in lin.tab}
lct: = nl;	write ('number of page is',
while vstx <= vspx do	(pgd + pfn-1): decposit (round (pgd + pfn)), ',');
begin	write ('it is now');
stepdelt (srng, xbin, sx);	timwrit (h, m, s, f); {displaying the page end time}
sound (1000); {sound signal}	write(', ');
delay (200); {****}	write(' end of ',pgn:decposit(round(pgn)), ' page,
nosound; {delta x}	');
sound (1000); {sound signal}	sound (750); {sound signal}
delay (200); {*****}	delay (500); {at the end}
nosound; {delta x}	nosound; {pages}
writeln(lin, 'dx = ',vstx:3);	pgn: = pgn + 1;
vsty:=0;	writeln ('start of', pgn: decposit (round (pgn)),
binreset(ybin);	'page');
· · · · · · · · · · · · · · · · · · ·	
vspy:=vstx;	writeln (lin);
aa: if vsty<=vspy then	writeln (lin, char (12)); {output disconnector out-
begin	put}
vdty:=vspy-vsty+1;	prnpgnum(pgn,lin);
bb: if (lct>=1)and(vsty<=vspy) then	lct:=nl;
begin	end;
if vdty>mx then ntd:=mx	goto aa;
else ntd:=vdty;	end;
nct:=ntd;	inc(vstx);
x=1;	bininc(xbin);
<pre>prnnttit(ntd,vsty,lin);</pre>	end;
resvect(emax,zmax);	write (lin, 'end of', pgn: decposit (round (pgn)),
while nct>=1 do	'page,'); {pgn page partner label output}
begin	write (lin, 'page computating time:'); {*****}
dz:=0;	gettime (h, m, s, f);
binreset(zbin);	dtimer (ph, pm, ps, pf, h, m, s, f, dh, dm, ds, df);
stepdelt(srng,ybin,sy);	prntime (dh, dm, ds, df, lin); {output of page time
while dz<=vsty do	in lin.tab}
begin	write ('number of page is',
stepdelt(srng,zbin,sz);	(pgd + pfn -1): decposit (round (pgd + pfn)), ',');
normerr(vstx,vsty,dz,sx,sy,sz,dnm);	write ('it is now');
sortvect(x,dz,dnm,emax,zmax);	timwrit (h, m, s, f); {displaying the page end time}
inc(dz);	write(', ');
bininc(zbin);	write(' end of ',pgn:decposit(round(pgn)), ' page,
end;	');
vdty:=vdty-1;	writeln('end of table');
vsty:=vsty+1;	sound (750); {sound signal}
x:=x+1;	delay (500); {at the end}
bininc(ybin);	nosound; {pages}
nct:=nct-1;	write (lin, 'end of table,',
end;	'table computating time:'); {table end label output}
onu,	table compatating time. j, table the label output

dtimer (th, tm, ts, tf, h, m, s, f, dh, dm, ds, df); prntime (dh, dm, ds, df, lin); {output of table time in lin.tab}

writeln (lin);

close (lin); {closing the lin.tab results file on the active disk}

sound (500); {sound signal} delay (1000); {at the end} nosound; {tables}

end

{/////// end of main program \\\\\\\\}

The values of  $\delta_i$  for  $i = 1 \div 5$  were determined. It is established that the maximum error  $\delta_n$  occurs twice in the process of interpolation of the line, and the directions of the vectors of the normal corresponding to  $\delta_n$ 

are opposite (one towards the other). The following relations are valid for the parameters  $\Delta y$ ,  $\Delta z$ ,  $y_o$  and  $z_o$ :

$$\begin{cases} \Delta y = \Delta z, \\ y_0 = z_0 \end{cases}$$
 (12)

In addition, it is established that:

$$\Delta x = 2\Delta y + 1$$
, для n-непарних;  $\Delta x = 2\Delta y$ , для n-парних.  $\Delta x = 2\Delta y$ 

Fig.5 shows the operation of the 3D linear interpolator on the digital integrator of sequential carry for  $\Delta x = 10$ ,  $\Delta y = 5$ ,  $\Delta z = 5$ , which corresponds to the maximum interpolation error at n = 4.

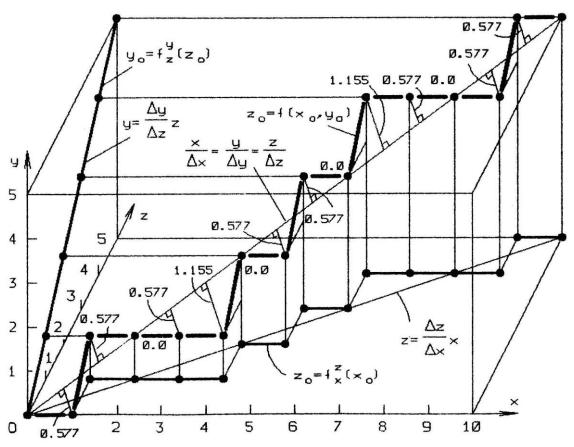


Fig.5. Overation of the 3D linear interpolator on the digital integrator of sequential carry for  $\Delta x = 10$ ,  $\Delta y = 5$ ,  $\Delta z = 5$ , n = 4

If we conditionally denote the number of pulses t at the input of the counter corresponding to the first appearance of the maximum error at i-pairs, as  $C^l$  i and the error as  $\delta_n^1$ , and the number of pulses corresponding to the second appearance of the maximum error as  $C^2$  and the error as  $\delta_n^2$ , then, taking into account projection of interpolation lines on the plane (yOz), it is proposed to assume that the number of input pulses  $C^l$  corresponds to a negative error  $\delta_n^1$ , and  $C^2$  - a positive error  $\delta_n^2$ . In the course of the performed analysis and on the basis of the principle of mathematical induction the iterative method of definition of parameters at which there is a

maximum error of 3D linear interpolation with use of DISC is offered:

1) if *i*-odd, then  $\Delta x_i = 2 \cdot \Delta x_{i-1} + 1$ ,  $\Delta y_i = \Delta z_i = \Delta x_{i-1}$ , a  $C_i^{\ I} = 2 \cdot C_{i-1}^2 + 1$ ,

 $C_{i}^{2}=C_{i-1}^{2}$ , and  $\Delta x_{i}=C_{i}^{1}$ , a  $\Delta y_{i}=\Delta z_{i}=\Delta x_{i-1}=C_{i}^{2}$ ;

2) if i-pair, then  $\Delta x_i = 2 \cdot \Delta x_{i-1}$ ,  $\Delta y_i = \Delta z_i = \Delta x_{i-1}$ , a  $C^l_{i-1} = C^l_{i-1}$ ,  $C^2_{i-2} = 2 \cdot C^l_{i-1}$ ,

and,  $\Delta x_i = C^2_i$ , a  $\Delta y_i = \Delta z_i = \Delta x_{i-1} = C^1_i$ .

If for  $x_0$  and  $y_0$ , corresponding to the number of pulses at the input  $C^l_i$ , take  $x^l_0$  and  $y^l_0$ , and for  $x_0$  and  $y_0$ , corresponding to  $C^2_l$ , take  $x^2_0$  and  $y^2_0$ , then the analysis follows from the analysis (14):

$$\begin{cases} \begin{bmatrix} x_0^1 - 2y_0^1 = 2n - 1, \\ 2y_0^2 - x_0^2 = 2n + 1; \end{bmatrix}^{\text{when } i - \text{ odd}} \\ \begin{bmatrix} x_0^1 - 2y_0^1 = n/2, \\ 2y_0^2 - x_0^2 = n/2; \end{bmatrix}^{\text{(14)}} \end{cases}$$

Given (12), the following is true:

$$\begin{vmatrix} \Delta y & \Delta z \\ -y_0 & -z_0 \end{vmatrix} \equiv 0.$$

Thus, expression (11) will take the form:

$$\delta_n = \frac{\sqrt{2} \cdot (\Delta x \cdot y_0 - \Delta y \cdot x_0)}{\sqrt{\Delta x^2 + 2 \cdot \Delta y^2}} . (15)$$

Taking into account (13) and (14) for pairs i, the expression for error (15) takes the form:

$$\delta_n^1 = -\frac{n}{2\sqrt{3}}; \delta_n^2 = \frac{n}{2\sqrt{3}}$$
 (16)

Taking into account (13), (14) and on the basis of (15) for odd i the following expressions (17) can be written:

$$\delta_n^1 = \frac{1}{\sqrt{3}} \left( \frac{2}{3} - \frac{n+1}{2} \right); \delta_n^2 = \frac{1}{\sqrt{3}} \left( \frac{1}{3} + \frac{n-1}{2} \right).$$
 (17)

As a result of the conducted researches and by means of the offered expressions (16) and (17) data on

the absolute maximum error of the 3D linear interpolator on DISC (tab. 1 and tab. 2) are received.

Let's analyze the error of the 3D linear interpolator on the DISC. The value of the relative error of 3D reproduction of a straight line is  $(\delta_0 / \sqrt{\Delta x^2 + \Delta y^2 + \Delta z^2}) \cdot 100\%$  and is a decreasing value: at n = 5 it is equal to 5.3%, and at n = 10 it is already equal to 0.35%.

In other words, the higher the discrete coordinate display space resolution, the less noticeable the absolute interpolation error. For example, for n=12 the maximum absolute error of the 3D interpolator is equal to 3.4641 discrete, the relative error is 0.10% (at n=12, the resolution of the 3D discrete coordinate display space is  $4096 \times 4096 \times 4096$  pixels).

The obtained values of the relative errors of 3D interpolation are much smaller in comparison with, for example, the errors of image output to the information display device screen, reaching values from  $0.4 \div 0.5\%$  to  $4 \div 5\%$  [2, 8, 10] and not related to the error interpolation. In addition, when using interpolators on the DISC, error occurs only at intermediate points of the segment of the straight line being reproduced. The beginning and end of the interpolation segment exactly coincide with the ideal boundaries of the segment, ie when constructing, for example, a broken line consisting of a sequence of segments, the error of interpolation coordinates of the beginning of the sides of the broken relative to their ideal coordinates will not accumulate.

Table 1. Error of the 3D linear interpolator on DISC, binary code  $\Delta x$ ,  $\Delta y$ ,  $\Delta z$  and  $C_i^{1,2}$  for  $n=2\div 16$ 

	binary code $\Delta x$ , $\Delta y$ , $\Delta z$ and $C_i^{1,2}$ for $n=2\div 16$						
	The value of $\Delta x$ ,		The number of pulses at the input of the counter C <sub>i</sub> <sup>1</sup> ,				
	value $\Delta y = \Delta z$		$C_i^2$				
n	Binary	Decimal	Binary	Decimal	$\delta_{n}$		
	SeniorsJuniors	Decimal	SeniorsJuniors	Decilliai			
2	10	2	10	1	0.5774		
2	01	1	01	2	0.3774		
3	101	5	010	5	0.7386		
3	010	2	101	2	0.7380		
4	1010	10	1010	5	1.1547		
4	0101	5	0101	10	1.1347		
5	10101	21	10101	21	1.3406		
5	01010	10	01010	10	1.5400		
6	101010	42	101010	21	1.7321		
U	010101	21	010101	42	1./321		
7	1010101	85	1010101	85			
′	0101010	42	0101010	42	1.9230		
8	10101010 01010101	170	10101010	85			
0	10101010 01010101	85	01010101	170	2.3094		
9	101010101 010101010	341	101010101	341	2.5015		
,	101010101 010101010	170	010101010	170	2.3013		
10	1010101010 0101010101	682	1010101010	341	2.8868		
10	101010101010101010101	341	0101010101	682			
10101010101 01010101010	1365	10101010101 01010101010	1365	3.0791			
	10101010101 01010101010	682	10101010101 01010101010	682			
12	101010101010 010101010101	2730	101010101010 010101010101	1365			
		1365	101010101010101010101010101	2730	3.7041		
13	1010101010101 0101010101010	5461	1010101010101 010101010101010	5461	3.6565		
13	1010101010101010101010101010	2730	1010101010101 01010101010101	2730	5.0505		

14	10101010101010 01010101010101	10922 5461	10101010101010 01010101010101	5461 10922 4.0415
15	101010101010101 010101010101010	21845 10922	101010101010101 010101010101010	21845 10922 4.2339
16	1010101010101010 0101010101010101	43690 21845	1010101010101010 010101010101010101	21845 43690 4.6188

Table 2. Error of 3D line interpolator on the DISC,

	$\Delta x$	, Δ <i>y</i> , Δ <i>z</i> ,		$y_o^2$ for $n=3\div16$	
n	$\Delta x$ ,	(1)	$C_i^{\ 1}$	$x_o^1 - y_o^1$	Error,
n	Δy=Δz	(2)	$C_i^2$	$x_0^2 - y_0^2$	$\delta_{\mathrm{n}}$
3	5	(2)	5	1 1	0.7386
3	2	(1)	2	4 1	0.7380
4	10	(1)	5	4 1	1 1547
4	5	(2)	10	6 —— 4	1.1547
5	21	(2)	10	6 —— 4	1.3406
3	10	(1)	21	15 — 6	1.5400
6	42	(1)	21	15 — 6	1.7321
0	21	(2)	42	27 —— 15	1./321
7	85	(2)	42	27 —— 15	1.9230
/	42	(1)	85	58 —— 27	1.9230
8	170	(1)	85	58 —— 27	2.3094
0	85	(2)	170	112 58	2.3094
9	341	(2)	170	112 58	2.5015
7	170	(1)	341	229 — 112	2.3013
10	682	(1)	341	229 — 112	2.8868
10	341	(2)	682	453 —— 229	2.0000
11	1365	(2)	682	453 —— 229	3.0791
11	682	(1)	1365	912 — 453	3.0791
12	2730	(1)	1365	912 — 453	3.4641
12	1365	(2)	2730	1818 — 912	3.4041
13	5461	(2)	2730	1818 — 912	3.6565
13	2730	(1)	5461	3643 — 1818	3.0303
14	10922	(1)	5461	3643 — 1818	4.0415
14	5461	(2)	10922	7279 — 3643	4.0413
15	21845 10922	(2)	10922	7279 — 3643	4.2339
13	21043 10922	(1)	21845	14566 — 7279	
16	43690 21845	(1)	21845	14566 — 7279	4.6188
	43090 21843	(2)	43690	29124 – 14566	4.0100

#### **Conclusions**

After analyzing the features of reproduction of straight line segments by the method of digital differential analyzer, the absolute value of the error of the algorithm for interpolation of straight lines in three-dimensional coordinate space - formulas (16) and (17); and moments of time of occurrence of this error - tables 2 and 3. It is revealed that it is admissible to use algorithm of 3D interpolators of segments of straight lines by a method of the digital differential analyzer taking into account requirements to accuracy in concrete application, for example, in real-time systems, simulators, in animation, in simulators that require maximum speed when changing the image, ie in the presence of dynamic images without strict requirements for the accuracy of image reproduction.

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## FIRE HAZARD ANALYSIS IN THE BUILDING OF THE MOE "SECONDARY EDUCATIONAL SCHOOL $N_0$ . 1" SARANSK

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# АНАЛИЗ ПОЖАРНОЙ ОПАСНОСТИ В ЗДАНИИ МОУ «СРЕДНЯЯ ОБРАЗОВАТЕЛЬНАЯ ШКОЛА №1» Г.О. САРАНСК

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#### Abstract

The article is devoted to the problems of fire safety in public buildings.

The solution of fire safety problems is possible only on the basis of a comprehensive analysis of the object of research-identifying factors that affect: the possibility of a fire; the spread and development of a fire; the rescue of people and property; the effectiveness of fire elimination.

Studies have found that the safety of public buildings requires more attention, because, as a rule, these are buildings with a mass presence of people.

#### Аннотация

Статья посвящена проблематике обеспечения пожарной безопасности в общественных зданиях.

Решение задач по обеспечению пожарной безопасности возможно лишь на основе комплексного анализа объекта исследования - выявления факторов, влияющих: на возможность возникновения пожара; на распространение и развитие пожара; на спасение людей и имущества; на эффективность ликвидации пожара.

Проведенными исследованиями установлено, что безопасность общественных зданий требует более пристального внимания, потому что, как правило, это здания с массовым пребыванием людей.

**Keywords:** fire safety system, regulatory requirements, automatic fire alarm system, warning system and management of evacuation of people in case of fire, smoke removal system, individual fire risk.

**Ключевые слова:** система обеспечения пожарной безопасности, нормативные требования, автоматическая пожарная сигнализация, система оповещения и управления эвакуацией людей при пожаре, система дымоудаления, индивидуальный пожарный риск.

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